



## Shipboard sea state estimation based on wave induced response measurements

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# Shipboard sea state estimation based on wave-induced response measurements



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26<sup>th</sup> September, 2017

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Department of Mechanical Engineering

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$$(EIv'')'' = q - \rho A \ddot{v} \int_a^b \epsilon \Theta + \Omega \int \delta e^{i\pi} \{2.718281828\} \chi^2 \sum_i \gg \Sigma!$$

# Agenda

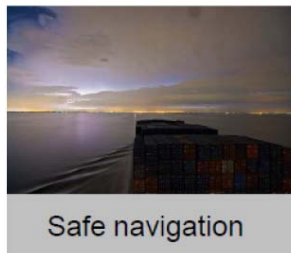
1. Introduction
2. Means for wave estimation
3. **Wave buoy analogy: Measured vessel responses**
  - Frequency and time domain procedures
4. Application studies
5. Final remarks



# Introduction: Areas of interest

Shipboard sea state estimation is relevant for, e.g.:

- **Safety of ships in transit and marine operations:** Structural integrity including fatigue damage; damage/loss of cargo; crew/passenger (dis)comfort
- **Dynamic positioning:** Better station-keeping capabilities, increased trust in operational windows
- **Environmentally friendly shipping:** Reduced exhaust emissions; improved fuel-efficiency, vessel and fleet performance systems
- **Wave and ocean statistics:** Continuous improvement of wave-scatter diagrams, better and/or more specific design of marine systems



# Introduction: Context

## Deterministic and statistical *short-term* response predictions

- *Deterministic predictions* → **5 – 90 seconds** ahead of instantaneous measurements; the actual response record is determined



*Heave compensation, helicopter landings, ...*

- *Statistical predictions* → **10 – 90 minutes** ahead of instantaneous measurements; statistics of the response record is determined



*Vessels in transit, risk avoidance...*

# Introduction: Application to DSS

## Decision support systems

- **Monitoring:** Displays weather and wave environment, motions, accelerations, hull girder strains, etc.
- **Statistical guidance:** Safe and efficient speed and course options.
- **Deterministic predictions:** What happens here-and-now



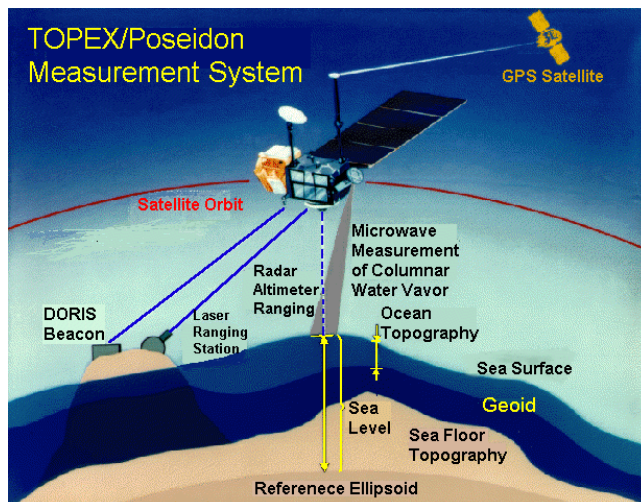
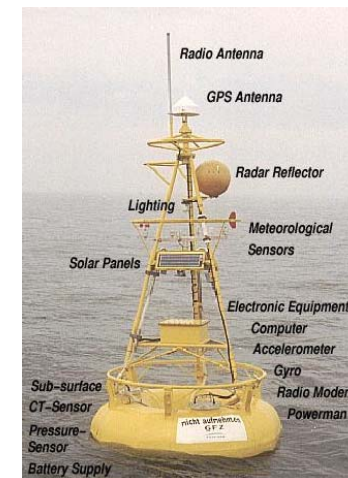
From K. Bendix , 05-03-2012 @ Skibsteknisk Selskab

**❑ Information about waves (= the sea state) is fundamental (or at least very valuable) to conduct safe and efficient marine operations!**

# Means for wave estimation (1/2)

**Well-known “typical” means to estimate sea states/wave energy spectra:**

- Wave rider buoys, satellite measurements, and wave radars
- Note, shipboard DSS requires the sea state to be continuously (10-20 min. basis) updated at the exact position of the moving vessel!
- **Wave buoys**; wave-induced motion (3 translations and 3 rotations) ‘transformed’ into measurements of wave
- Suffers from being at a fixed position, and the information from wave buoys is scars in many parts of the oceans.

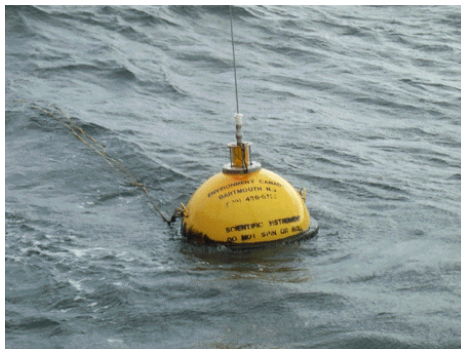


- **Satellite measurements**; valuable tool for statistics of ocean wave systems
- Processing time is (too) long i.e. satellite measurements are not applicable to DSS (yet...)



## Means for wave estimation (2/2)

- **Wave radar systems** provide sea state in real-time and the exact position of the vessel.
- Accurate and reliable on period and direction but not always on wave height
- Systems are somewhat expensive and require careful calibration.



A wave buoy is a **floating structure**; and so is any type of ship... **The wave buoy analogy**

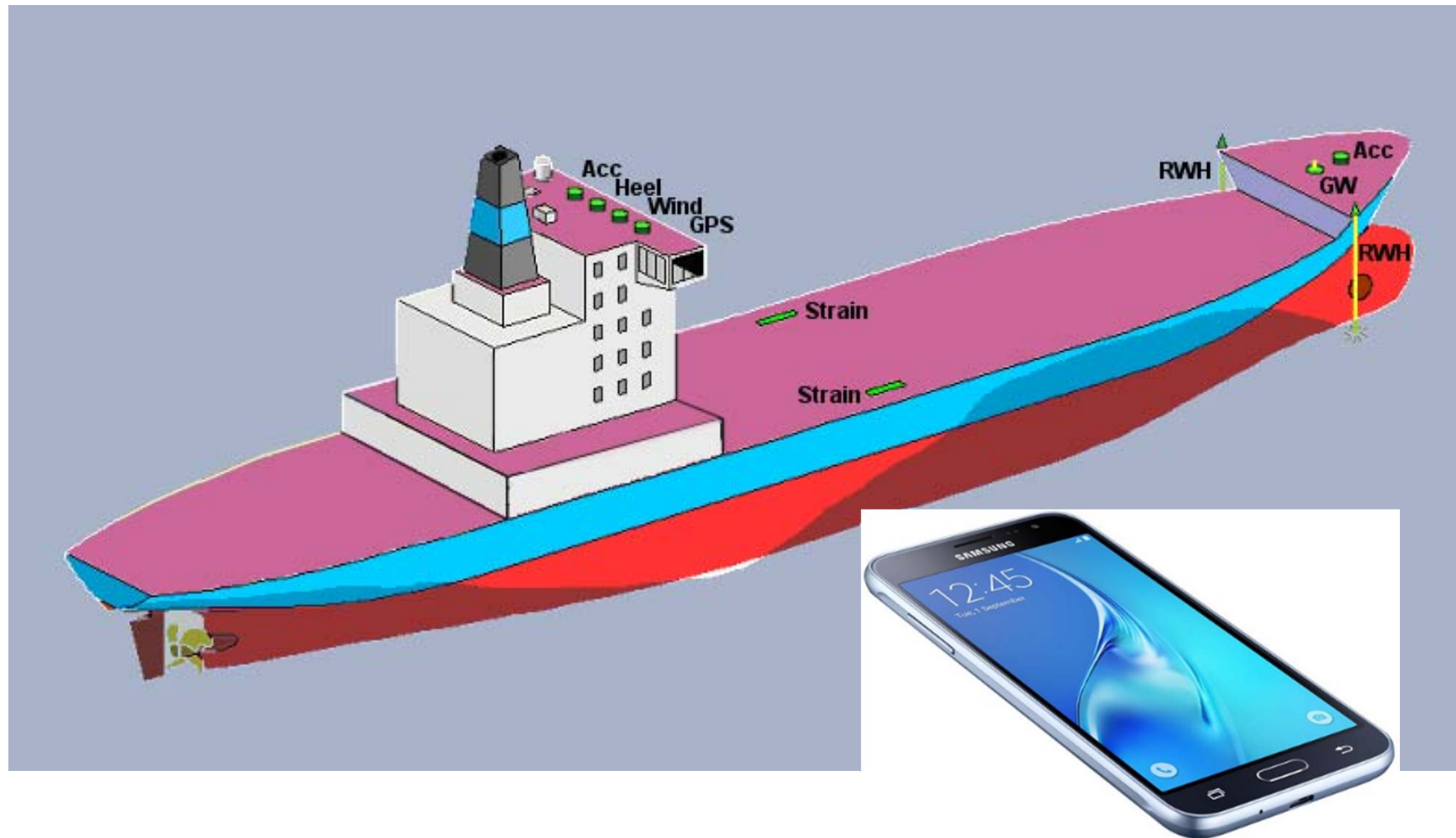
- Making use of available sensor recordings, i.e. no additional instrumentation or hardware
- Requires little calibration



# Wave buoy analogy

## Sea state estimation based on measured ship responses

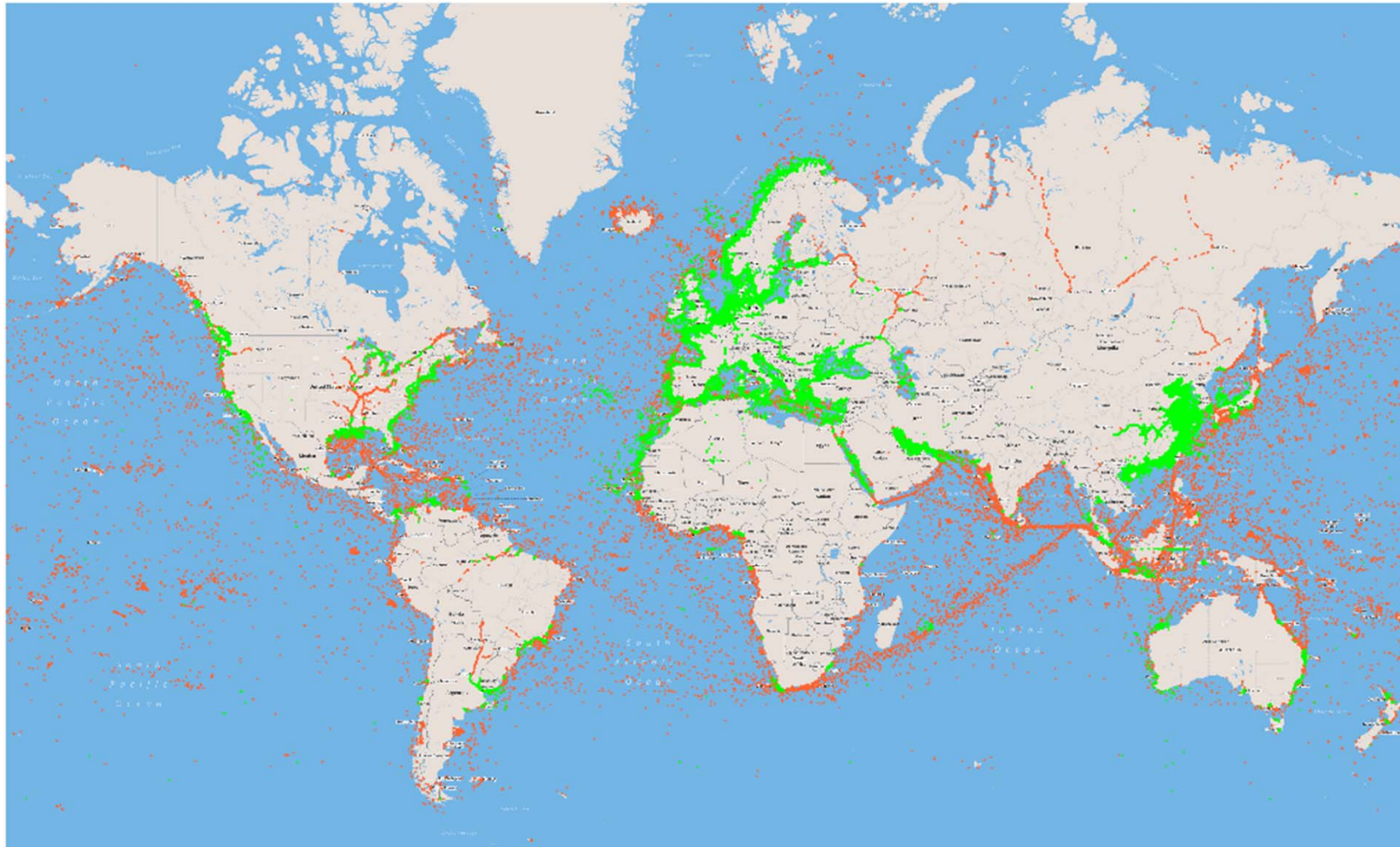
(recordings from a number of sensors...)



The future **Motion Response Unit...**

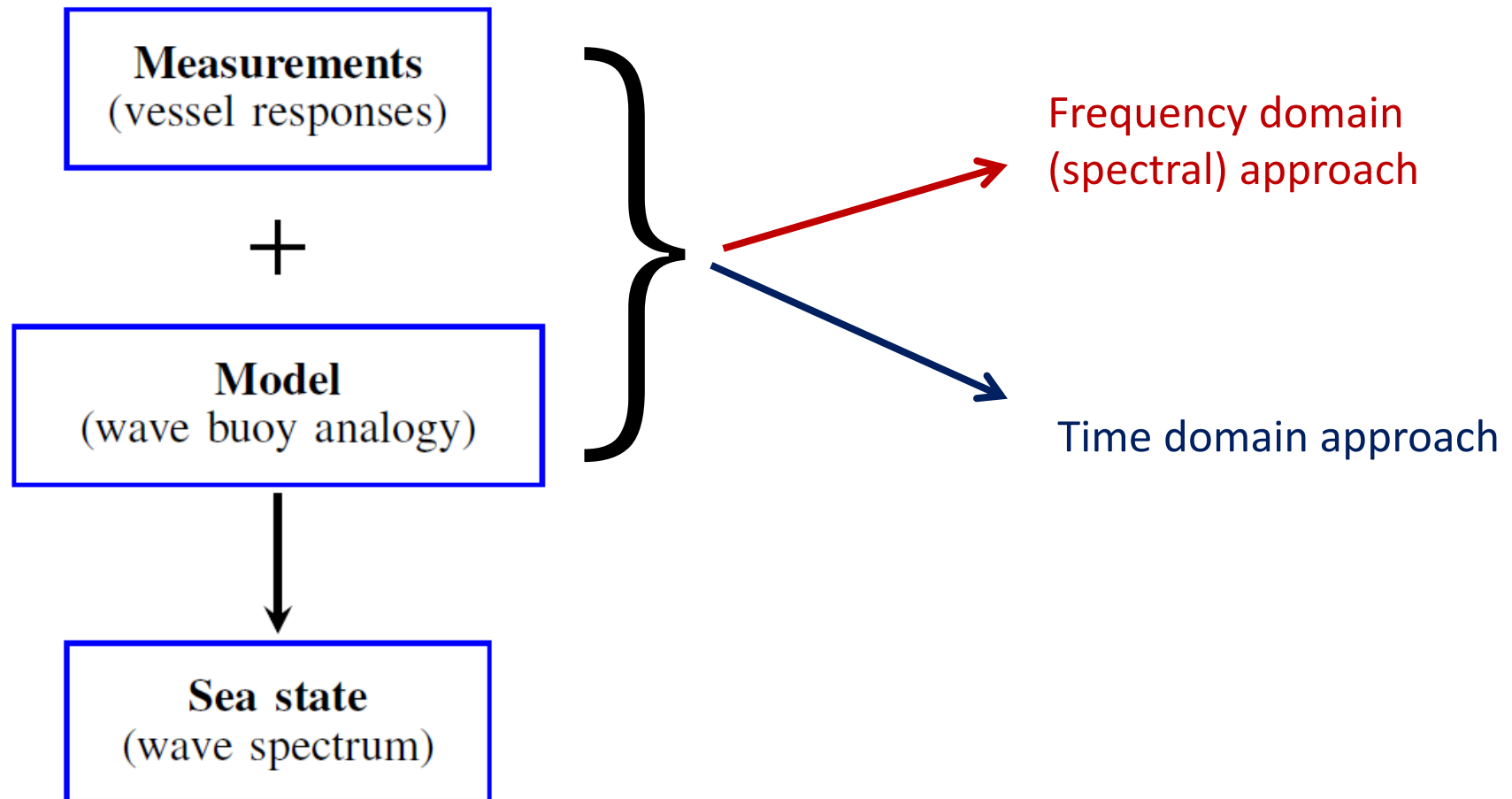
# Why the wave buoy analogy?

The amount of wave-induced data from vessels is huge...



A snapshot of vessel positions around the world's ocean based on AIS data (green: terrestrial, red: satellites) url: <https://www.fleetmon.com/global-vessel-coverage/>

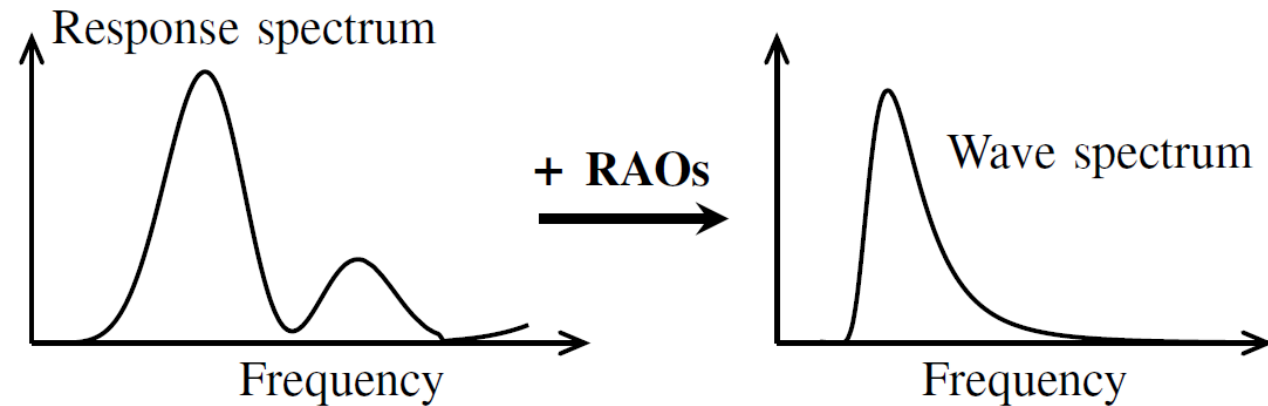
# Basic principle



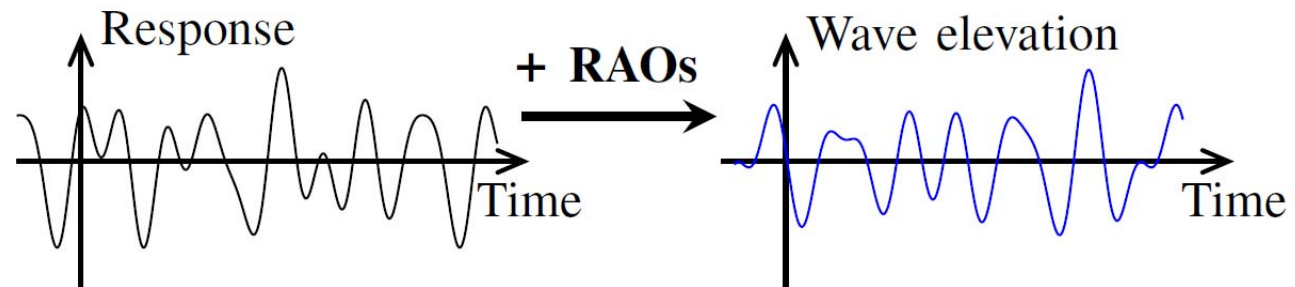
# Basic principle, cont'd

The wave buoy analogy is formulated in one of two domains:

Frequency domain  
(spectral approach):

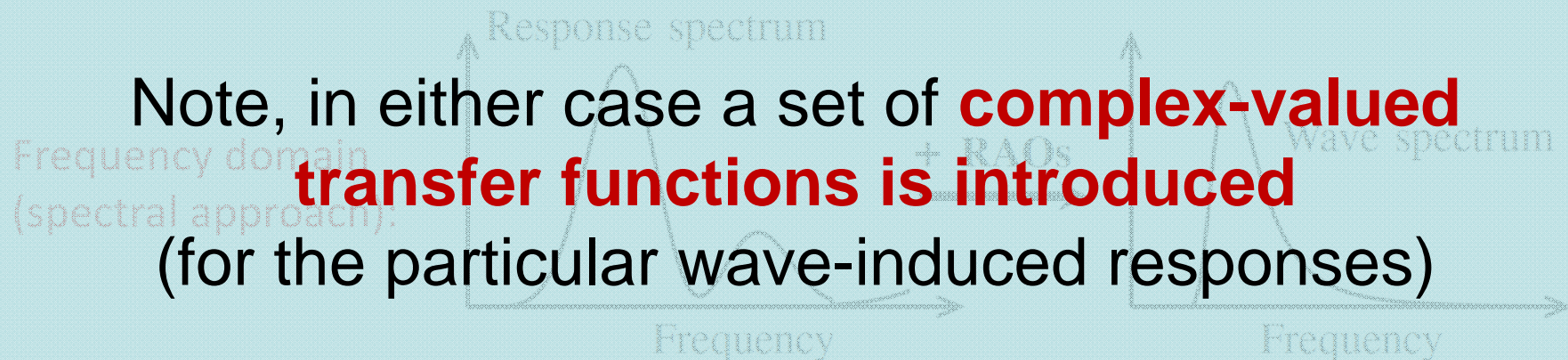


Time domain:



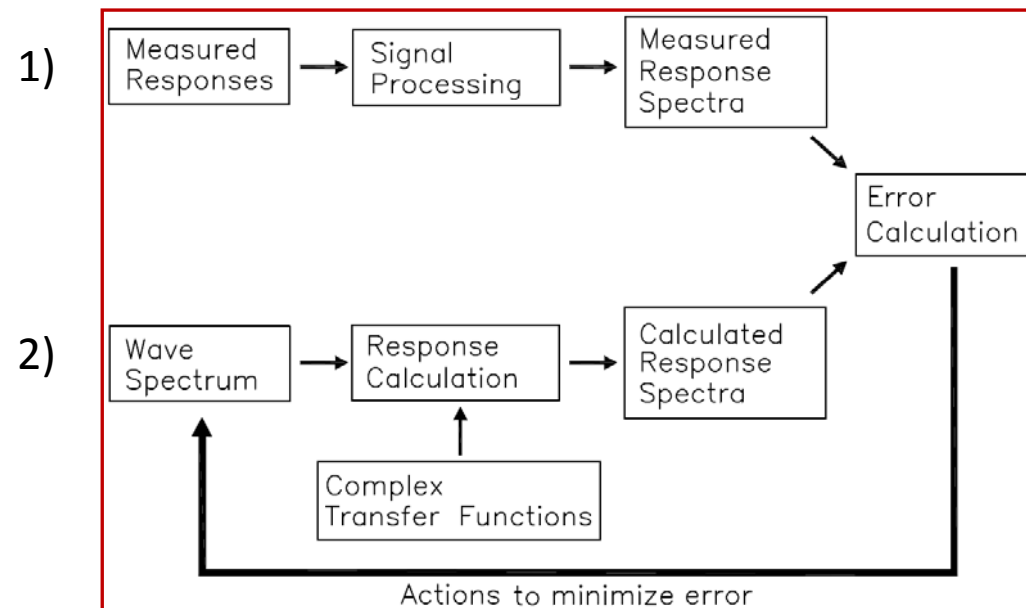


The wave buoy analogy is formulated in one of two domains:



- The majority of past work is focused on formulations in the frequency domain. NB. Strictly said, stationary conditions must apply.
- Time domain procedures can be formulated to relax the assumption about stationary conditions... work is still needed

# Wave buoy analogy: Frequency domain procedures



1) Measurements: from measured ship responses, response spectra are derived.

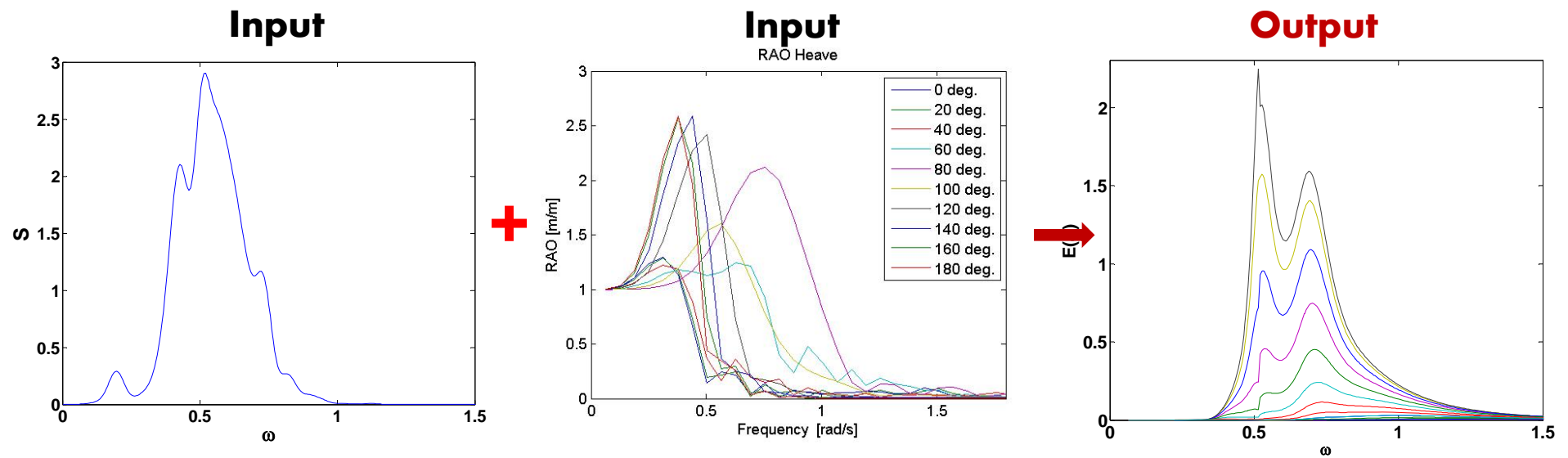
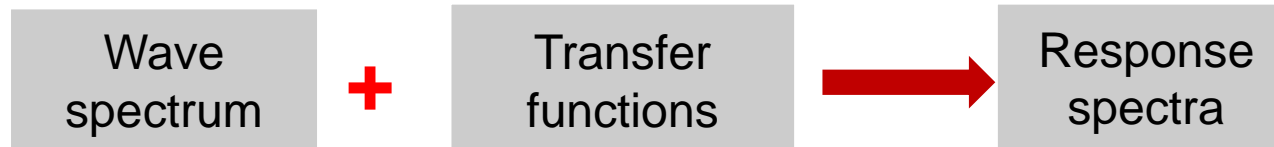
2) Calculations: by combination of a wave spectrum and linear transfer functions of the responses, response spectra are *calculated*.

- **Assumption**: Linear relationship between wave excitations and ship responses → i.e. wave-vessel transfer functions are used.
- Representations by parametric and non-parametric modelling and a novel 'brute-force residual-based' approach. Several studies have been made. Solutions exist with and without forward speed.
- **Note**: Estimations are, in theory, less reliable during severe sea states (non-linearity between excitations and responses...), but in practice...

# An illustration (1/2)

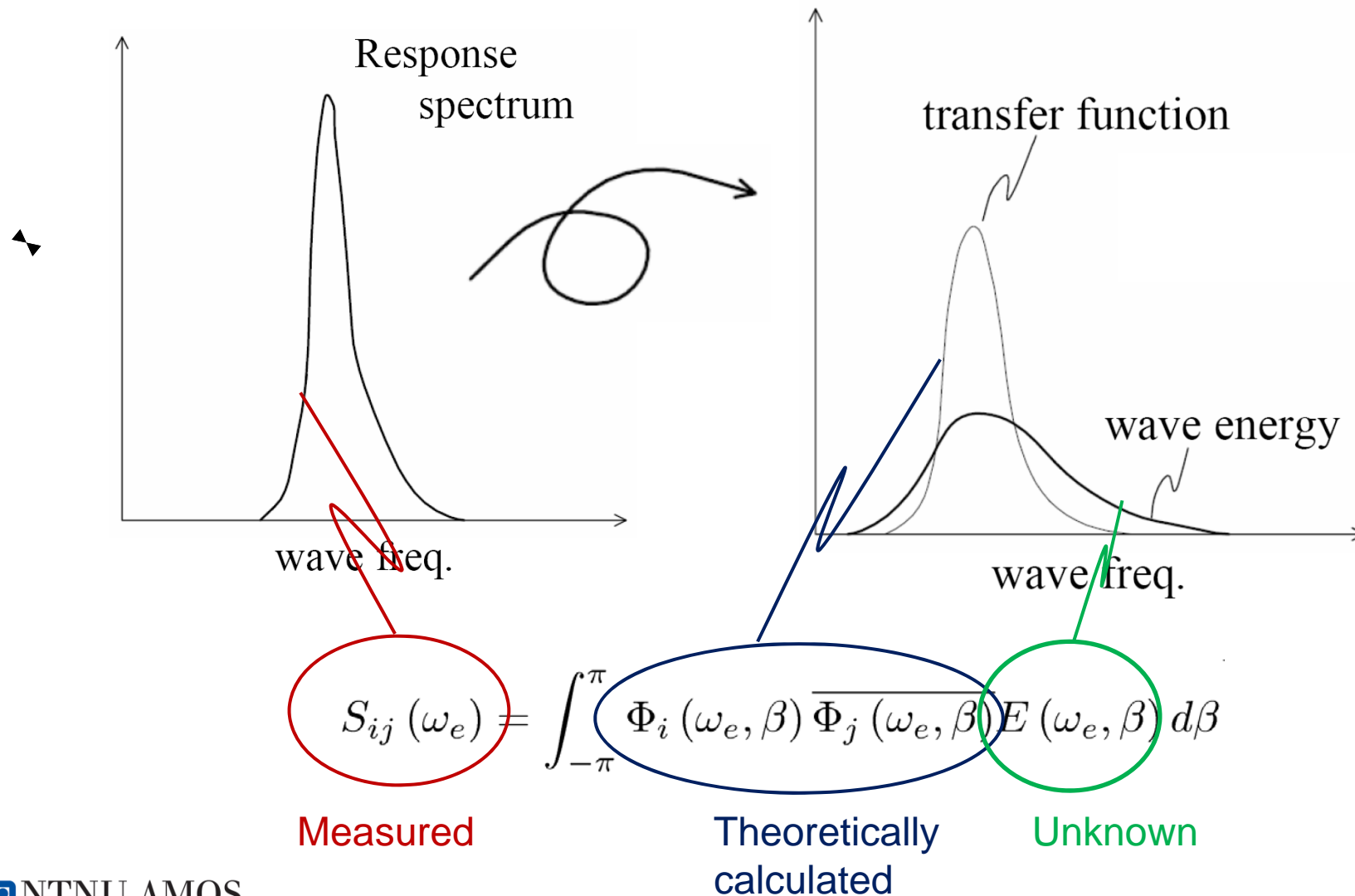
## Calculation of wave-induced responses:

Theoretically  
calculated



## An illustration (2/2)

The “inverse” process - i.e. the wave buoy analogy:





# In practice

Three wave-induced responses are measured simultaneously:

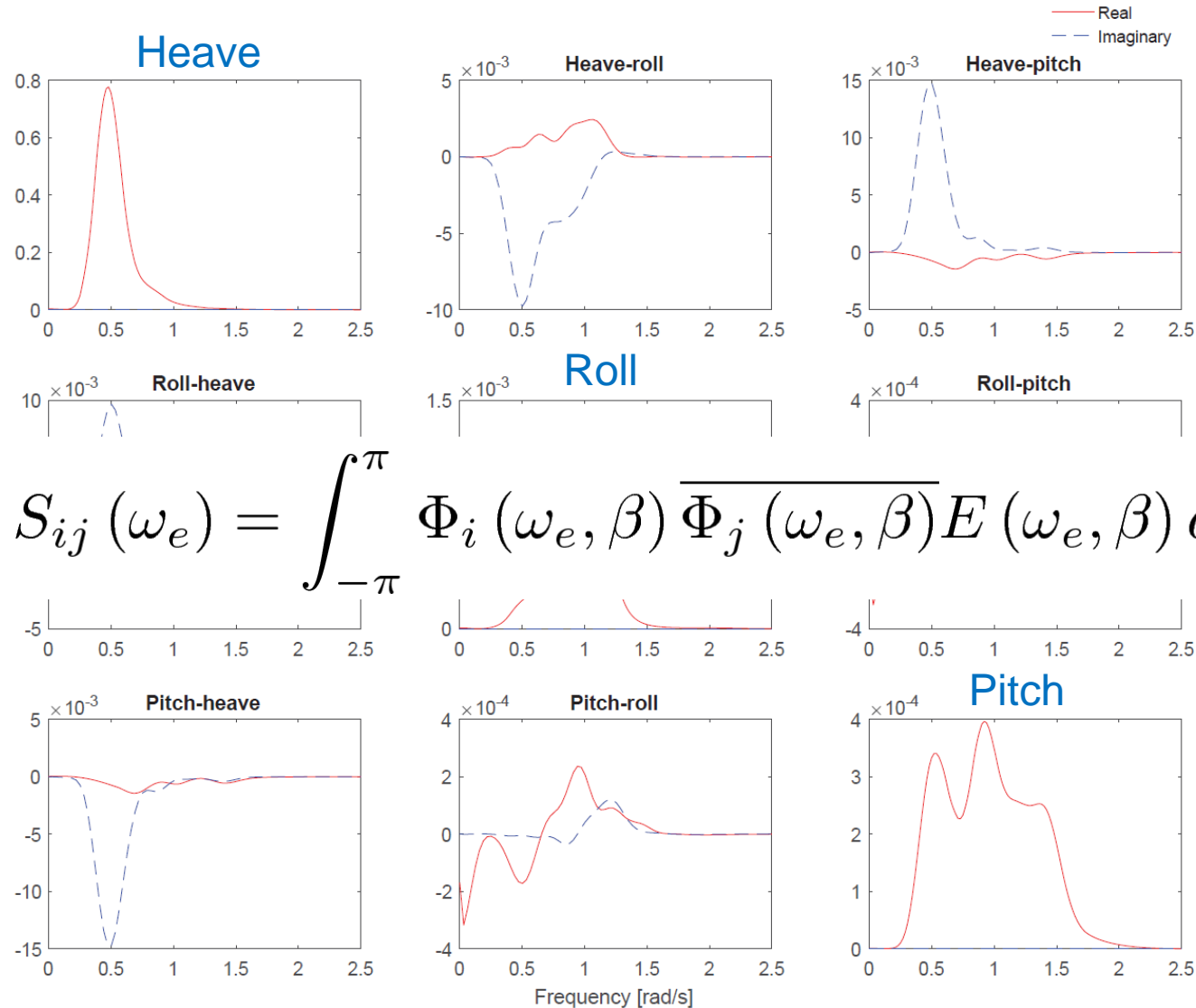
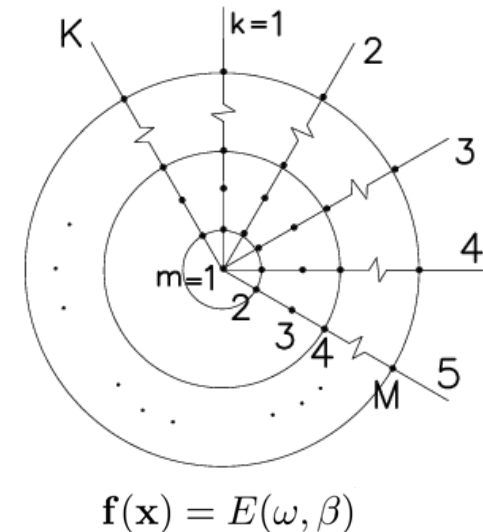


Figure 1: Cross spectra  $R_{ij}$  calculated from measured responses in heave [m], roll [rad.] and pitch [rad.]

## Three solution procedures:

### 1) Non-parametric (Bayesian) modelling

- In general, more unknowns than equations.
- Assumptions: 1) Introduction of the error as white noise (stochastic viewpoint); 2) Non-negativity constraint; 3) Introduction of prior information (~ 'Bayesian approach').



### 2) Parametric modelling

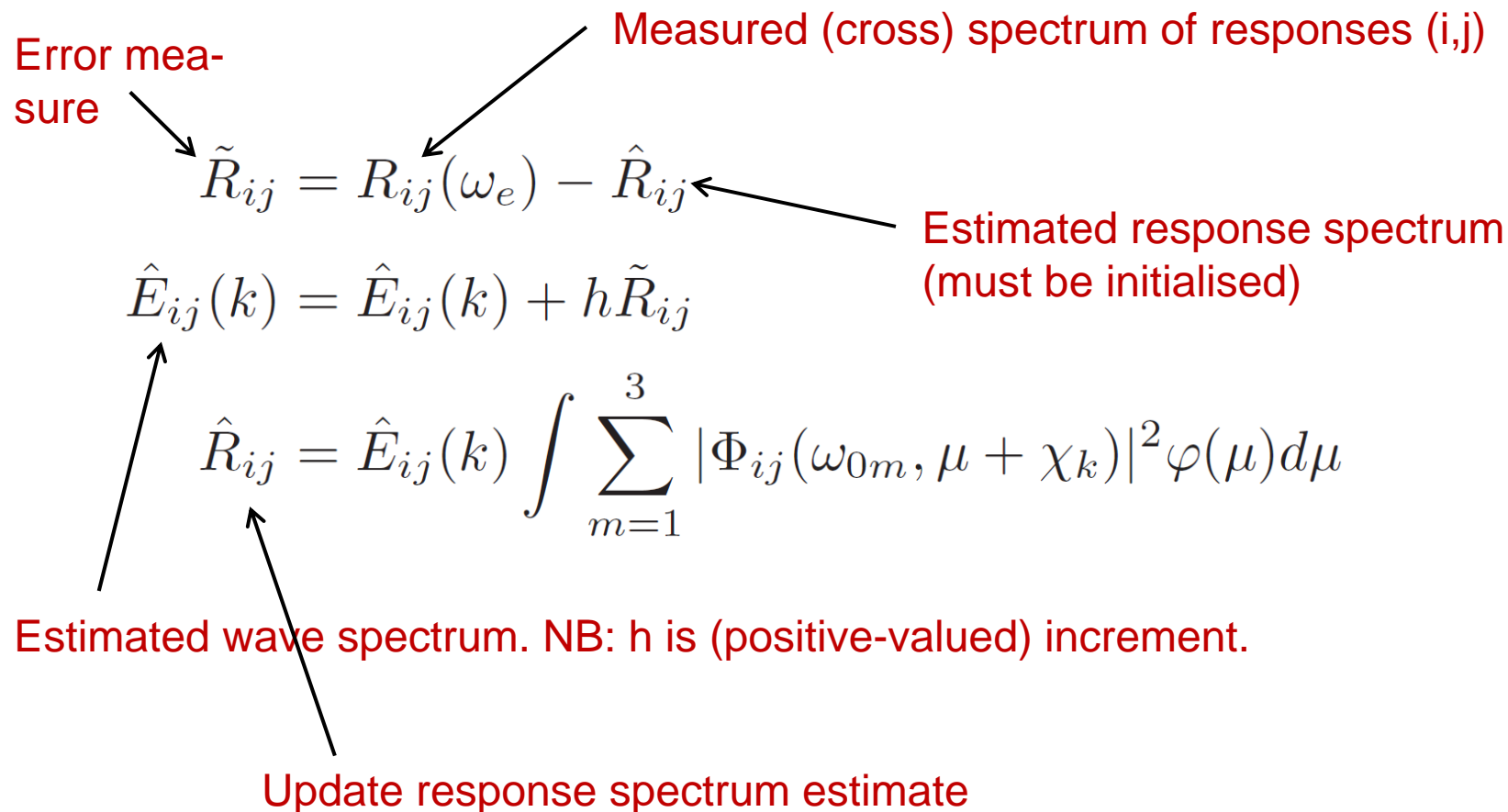
- Introduction of parameterised wave spectrum, e.g.:

$$E(\omega, \theta) = \frac{1}{4} \sum_{i=1}^3 \frac{\left( \frac{4\lambda_i + 1}{4} \omega_{p,i}^4 \right)^{\lambda_i}}{\Gamma(\lambda_i)} \frac{H_{s,i}^2}{\omega^{4\lambda_i + 1}} A(s_i) \cos^{2s_i} \left( \frac{\theta - \theta_{mean,i}}{2} \right) \exp \left[ -\frac{4\lambda_i + 1}{4} \left( \frac{\omega_{p,i}}{\omega} \right)^4 \right]$$

- I.e., the solution is a set of optimised wave parameters.

# Modelling approaches in frequency domain

## 3) A brute-force residual-based calculation using an iterative scheme (Nielsen et al., 2017a)



## 3) A brute-force residual-based calculation using an iterative scheme (Nielsen et al., 2017a)

$$\tilde{R}_{ij} = R_{ij}(\omega_e) - \hat{R}_{ij}$$

$$\hat{E}_{ij}(k) = \hat{E}_{ij}(k) + h\tilde{R}_{ij}$$

$$\hat{R}_{ij} = \hat{E}_{ij}(k) \int \sum_{m=1}^3 |\Phi_{ij}(\omega_{0m}, \mu + \chi_k)|^2 \varphi(\mu) d\mu$$

The iteration continues until the error measure,  $\tilde{R}_{ij}$ , attains a value below a specified threshold...

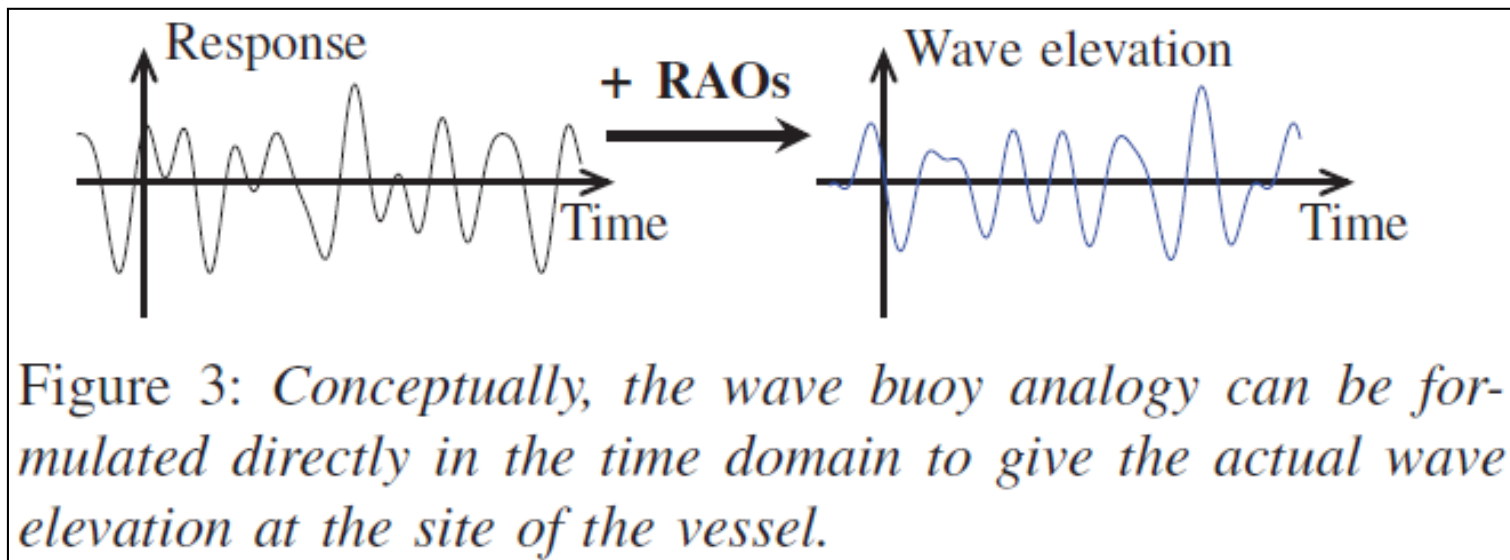


# Wave buoy analogy: Time domain procedures



- Sea state estimations in frequency domain depend highly on the spectral (response) analysis.
- In principle, stationary operational conditions are necessary because a minimum time window (10-15 min.), is needed to obtain reliable results from the spectral analysis.
- In practice, conditions are not stationary because of a changing sea state and/or, more likely, as a result of speed or heading changes of the vessel.
- In turn, sea state estimates (or updates) will be “back-dated”.
- Altogether, the sea state estimate may be compromised!
- Another approach: Sea state estimation in time domain! New and ongoing work on two different procedures: 1) Kalman filtering and 2) a stepwise procedure

# Modelling approaches in the time domain



The theoretical models; considering only one wave component:

Wave elevation: 
$$\zeta(t) = \zeta_a \cos(\omega t + \varepsilon)$$
$$= \text{Re}[(x_1 + ix_2)e^{i\omega t}]$$

Response: 
$$R(t) = \text{Re}[(H(\omega) + iH(\omega))(x_1 + ix_2)e^{i\omega t}] \quad \text{Eq. (A)}$$

## 1) Kalman filtering:

- The in-phase and quadrature components ( $x_1, x_2$ ) are introduced as the states at discrete time  $k$

$$\text{STATE EQUATION: } \begin{cases} x_1(k+1) = x_1(k) + \xi_1(k) \\ x_2(k+1) = x_2(k) + \xi_2(k) \end{cases}$$

- The measurement equation follows directly from Eq. (A) on slide 14:

$$\begin{aligned} \text{OUTPUT EQUATION: } z(k) &= (\text{Re}\{H(\bar{\omega})\} \cos(\bar{\omega}kT_s) - \text{Im}\{H(\bar{\omega})\} \sin(\bar{\omega}kT_s)) x_1(k) \\ \text{("measurement eq.") } &\quad - (\text{Re}\{H(\bar{\omega})\} \sin(\bar{\omega}kT_s) + \text{Im}\{H(\bar{\omega})\} \cos(\bar{\omega}kT_s)) x_2(k) + \theta(k) \end{aligned}$$

- Formulated in a vector-setting, the *standard prediction and update cycles* of the Kalman filter are applied to solve for the set of states at any discrete time

# Modelling approaches in the time domain

## 2) The stepwise procedure (Nielsen et al., 2015+2016):

- The method estimates, stepwise, (peak) frequency and, subsequently, wave amplitude and phase on batches of data (4-8 periods).
- For the single batch, nonlinear least squares (NLLS) fitting is used to fit a 'best average regular' wave.
- Updates made on at discrete times and, hence, the signal can be reconstructed.

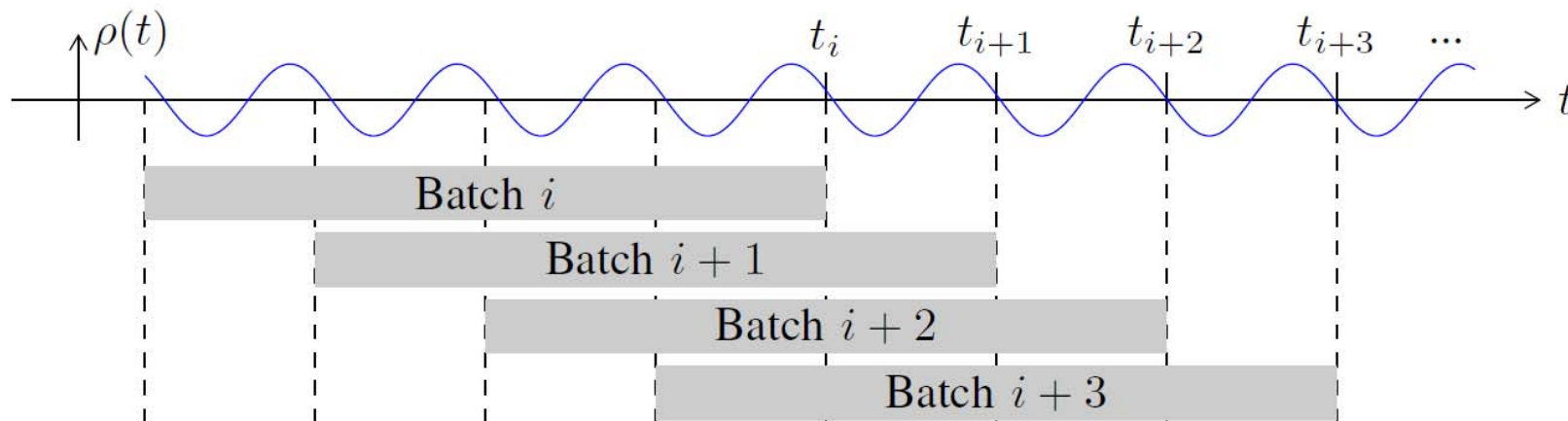
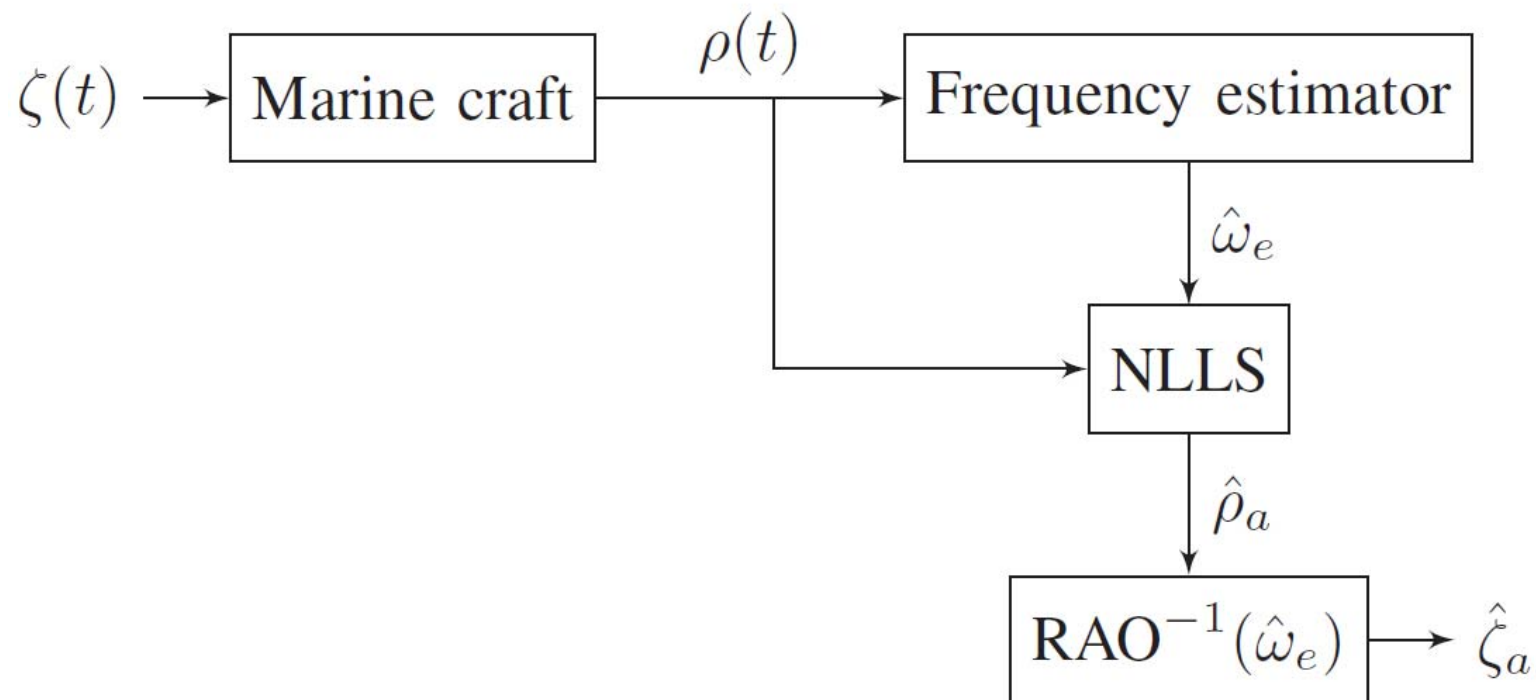


Figure 5: Batch data with 75% overlap. Batch  $i$  is processed at time  $t_i$ . [20]

# Modelling approaches in the time domain

2) The stepwise procedure (Nielsen et al., 2015+2016):

- The method estimates, stepwise, (peak) frequency and, subsequently, wave amplitude and phase on batches of data (4-8 periods)..

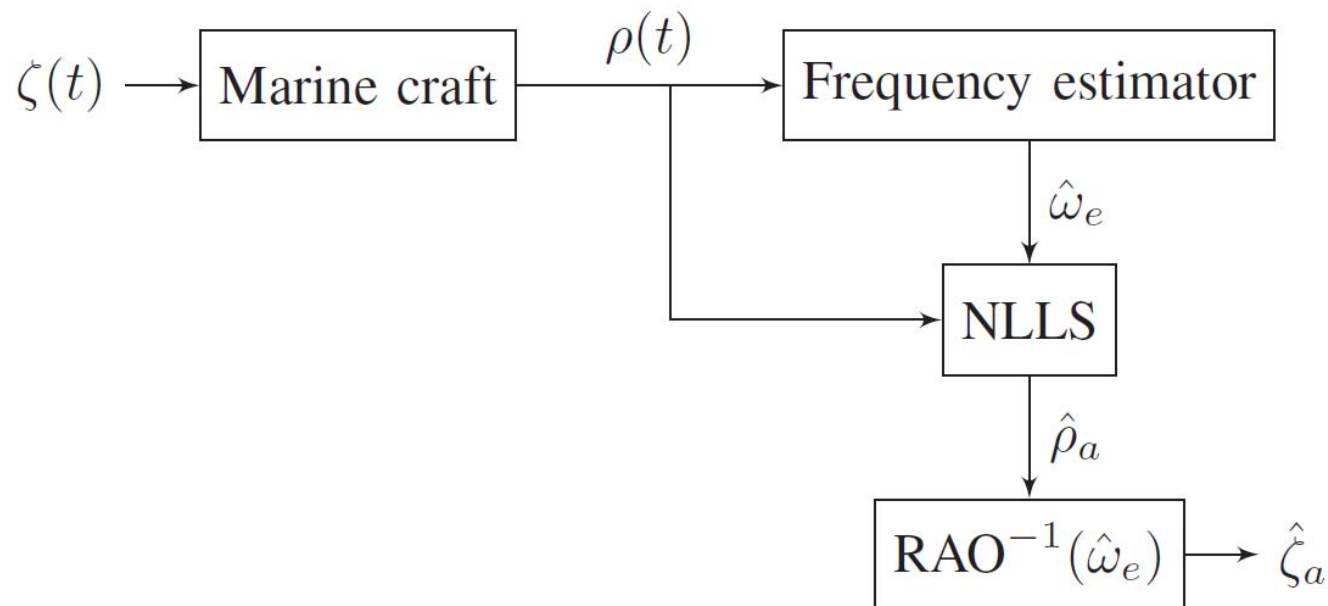




# Modelling approaches in the time domain

## 2) The stepwise procedure (Nielsen et al., 2015+2016):

- The method estimates, stepwise, (peak) frequency and, respectively, wave amplitude and phase on batches of data (4-8 periods).
- So far only regular (sinusoidal) waves can be considered.



✓ Frequency domain procedures are well-tested with both simulated data and full-scale measurements:

- 1) Dedicated sea trials (APOR'12)
- 2) In-service container vessel (PRADS'13)
- 3) Dedicated sea trials (ICASSP'18)

❖ Time domain procedures have been tested only using numerical simulations\*:

- 1) Kalman filtering at zero-forward speed; with forward speed results are developed only for head sea
- 2) Stepwise (NLLS) procedure only for regular waves at zero-forward speed
  - PhD work (proposal) to address specifically these issues

\* Limited literature shows results with experimental data.

# Dedicated sea trials (APOR'12)

## Full-scale measurements from sea trials (DRDC)



Fig. 2: The Canadian Navy research ship CFAV Quest.  
( $L = 71.6$  m,  $B = 12.8$  m,  $T = 4.8$  m,  $C_b = 0.51$ )

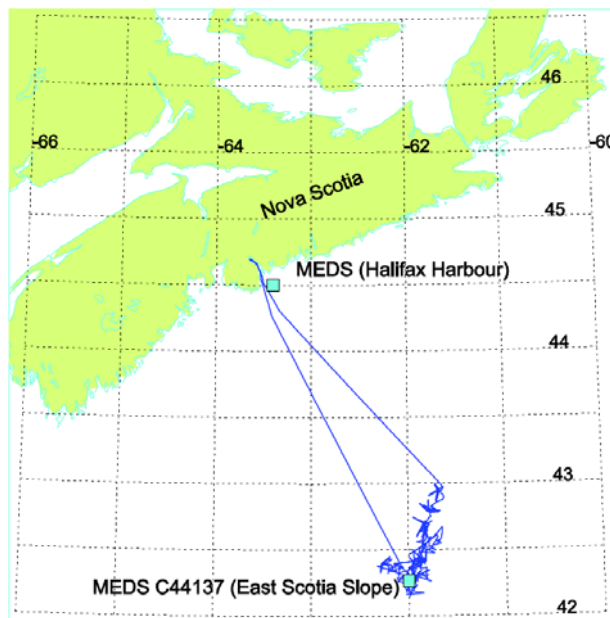


Fig. 3: Voyage map of sea trials.

- Responses: roll rate, roll angle, pitch rate, pitch angle, horizontal acc. and vertical acc. (all recorded at bridge).
- Ship motions calculated in-house by DRDC (SHIPMO7) using 2D strip theory
- Sea state monitored continuously by three wave buoys (MEDS C44137 and two drifting Triaxys buoys)
- 16 sets of trials, all with identical “relative” run patterns

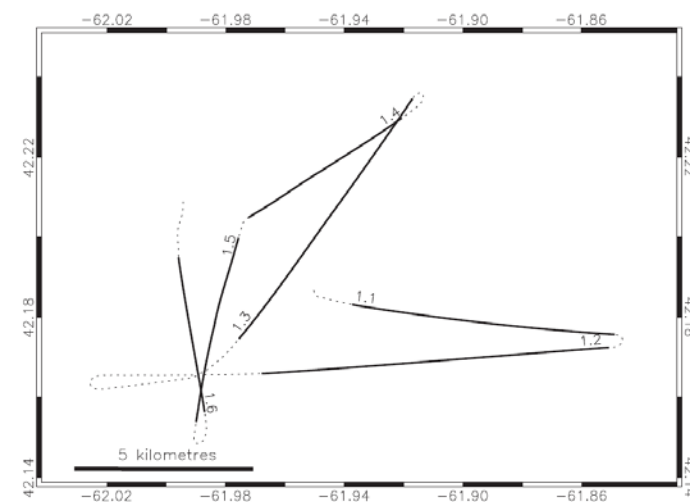
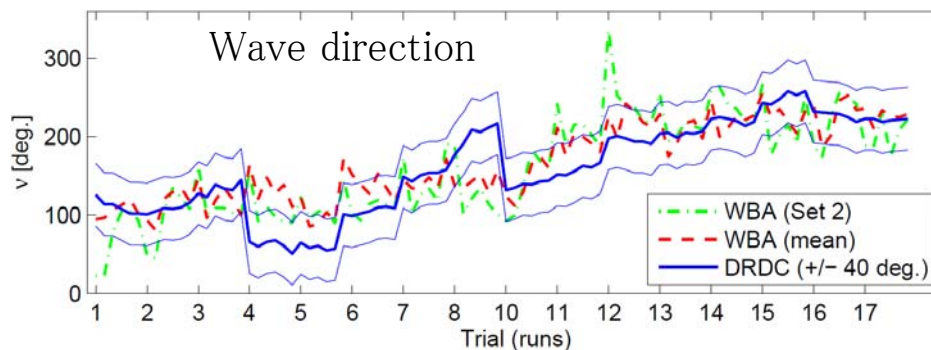
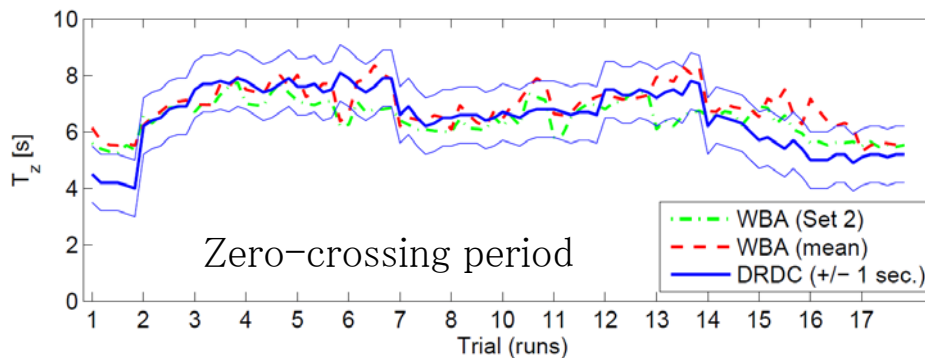
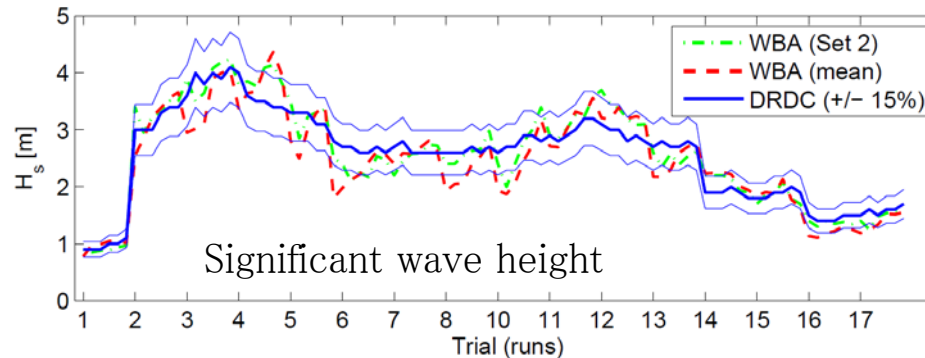


Fig. 4: Run pattern of trial no. 1.

# Dedicated sea trials (APOR'12)

## Full-scale measurements from sea trials (DRDC)



**WBA:** Results by wave buoy analogy (parametric modeling). NB. Combination of different sets of motion responses.

**DRDC:** Results obtained as the weighted average value of three floating wave rider buoys.

# Full-scale response measurements (PRADS'13)



**Table 1: Main dimensions of ship.**

Parameter	Dimension
$L_{OA}$	349.0 m
Beam	42.8 m
Draught	15.0 m
DWT	113,000 ton

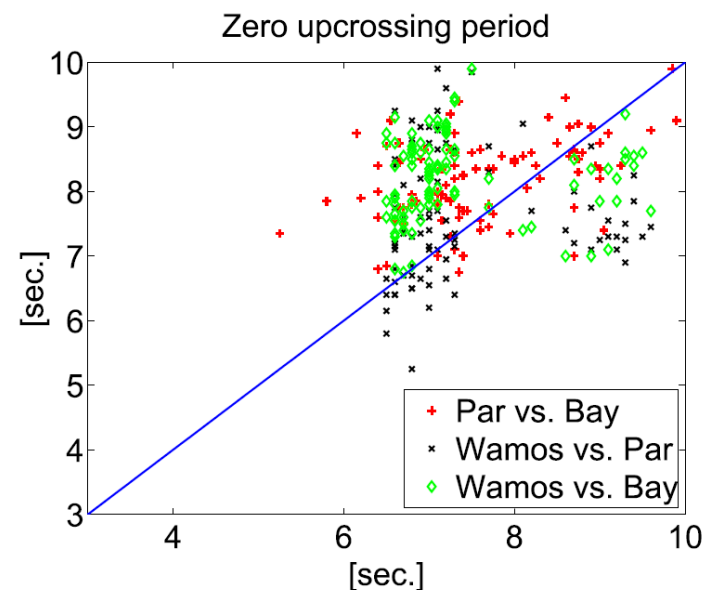
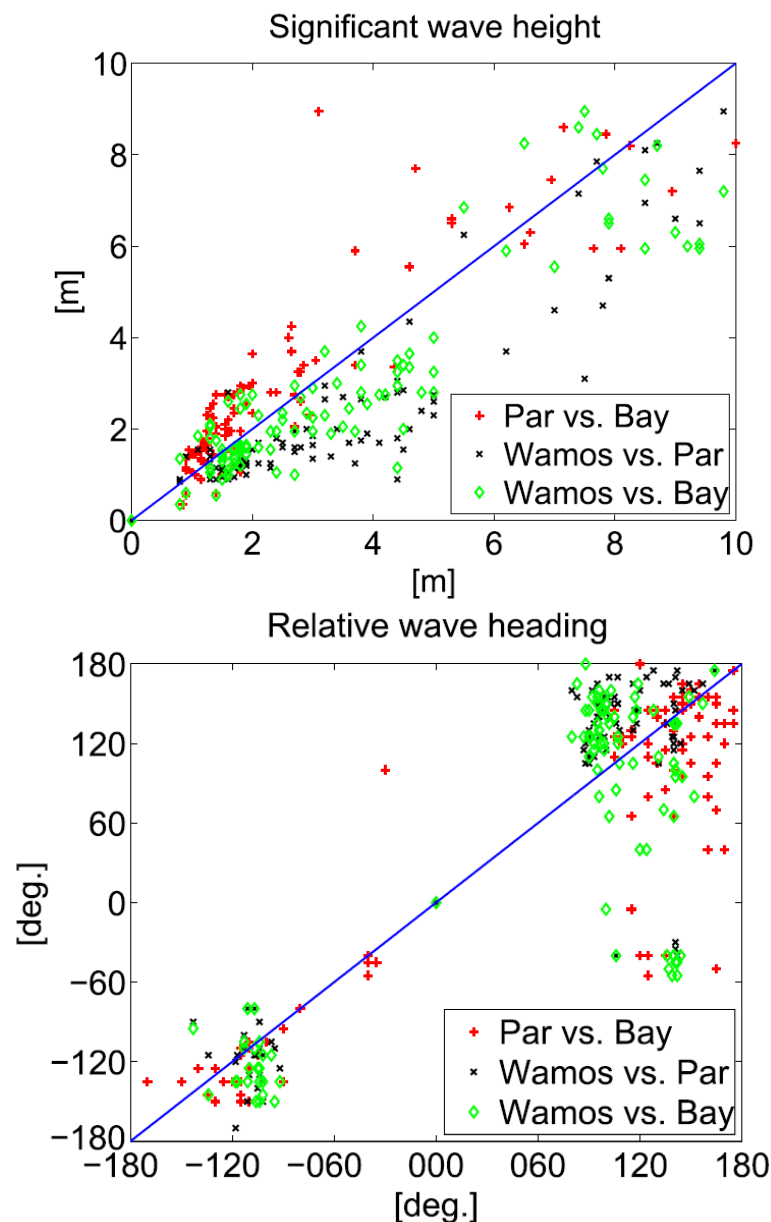
## Vessel responses:

- motions (sway, heave, roll, and pitch)
- accelerations
- dist. to sea surface
- strains





# Full-scale response measurements (PRADS'13)



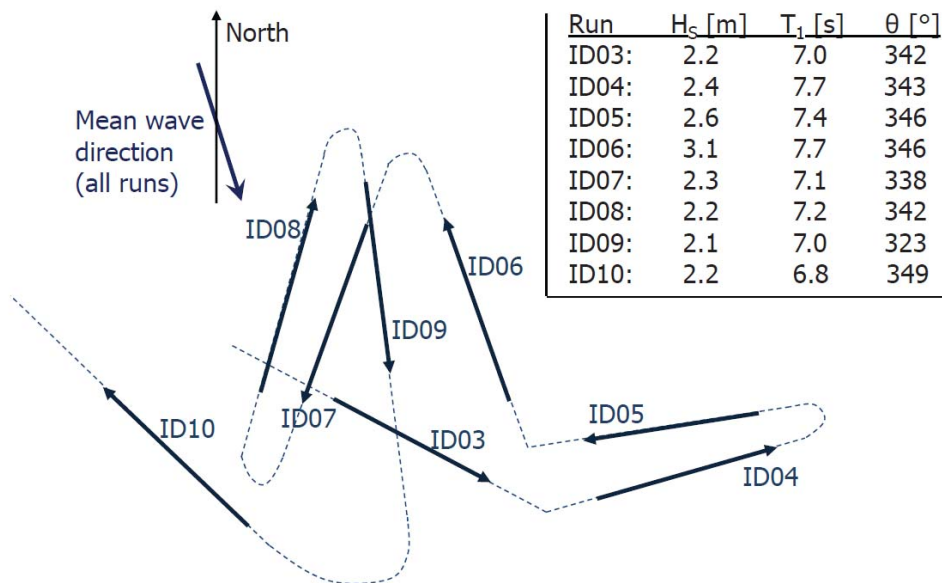
Correlation between estimates of integrated wave parameters as obtained by different shipboard techniques, including parametric (PAR) and Bayesian (Bay) modelling, respectively, and wave radar (Wamos).

# Dedicated sea trials (ICASSP'18)

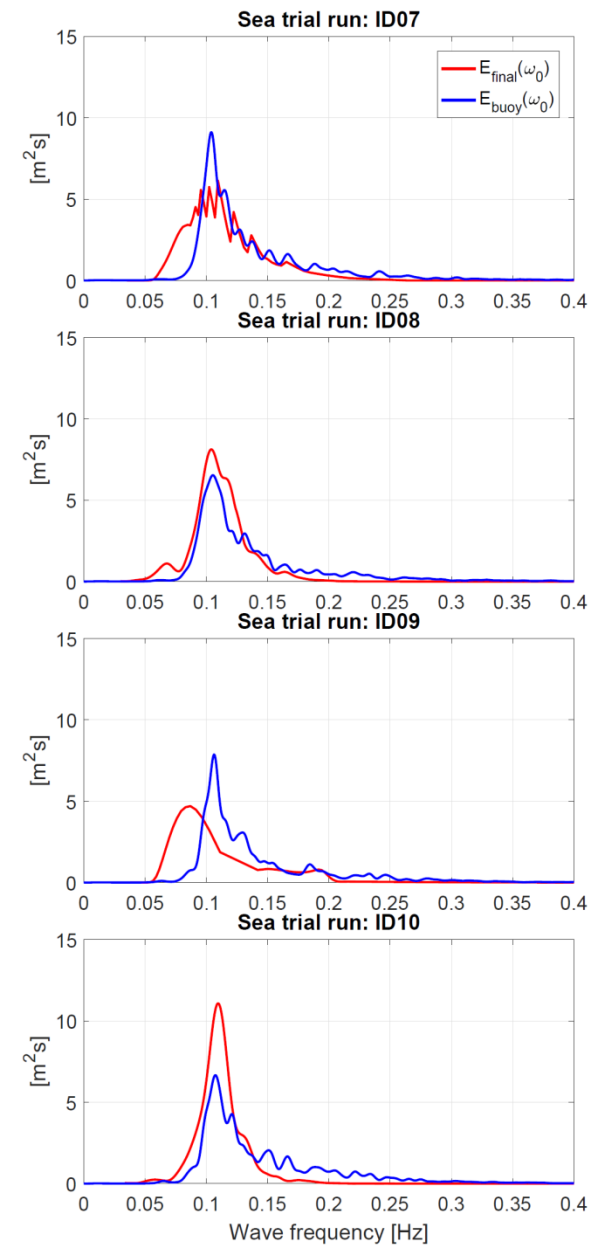
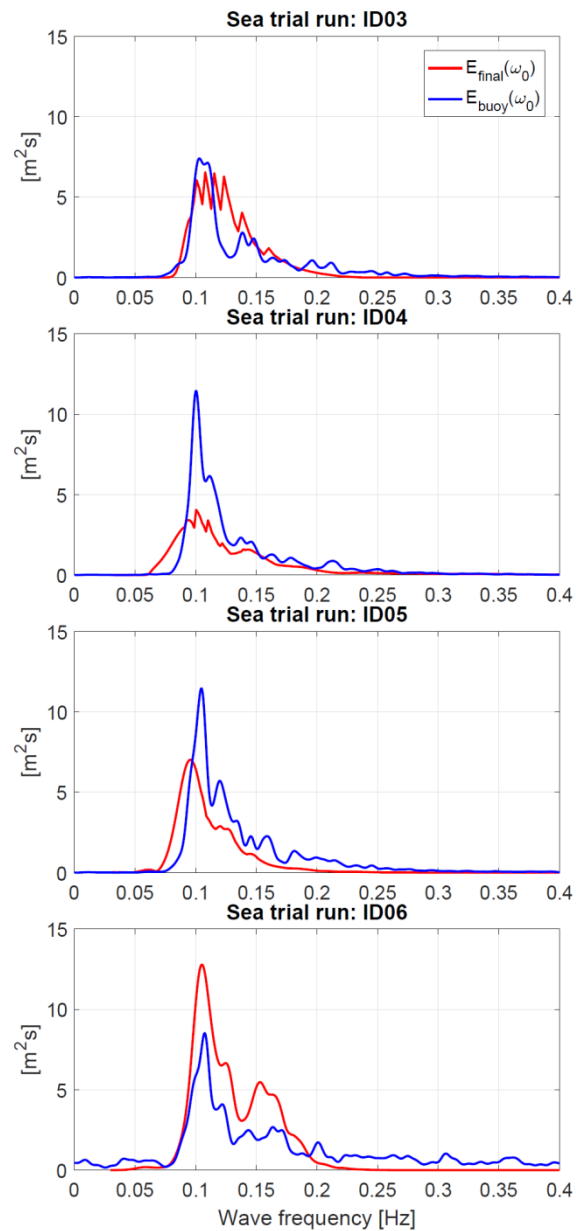


**Table 1.** Main parameters of research vessel (R/V Gunnerus).

Length, $L_{pp}$	28.9 m
Breadth, $B$	9.6 m
Draught, $T$	2.7 m
Block coefficient, $C_B$	0.56 [-]
Waterplane coefficient, $C_{WP}$	0.84 [-]
Displacement, $\Delta$	417 000 kg
Transverse metacentric height, $GM_T$	2.66 m



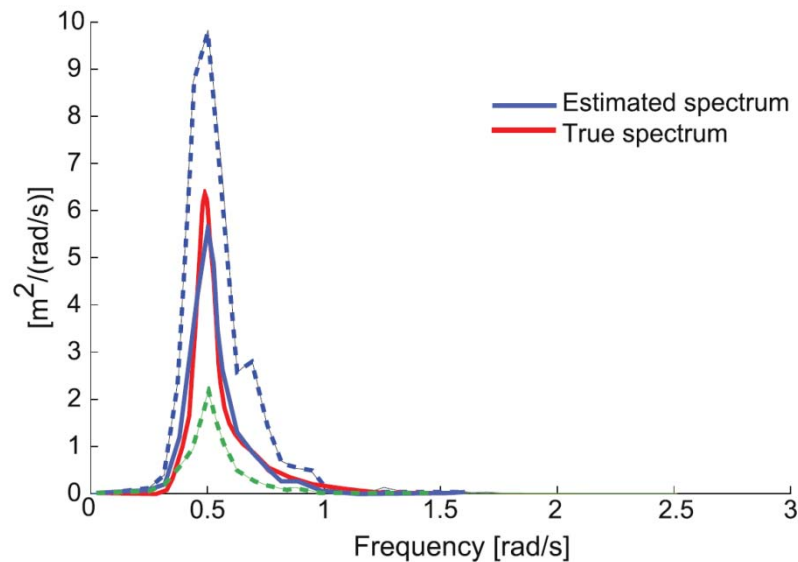
# Dedicated sea trials (ICASSP'18)



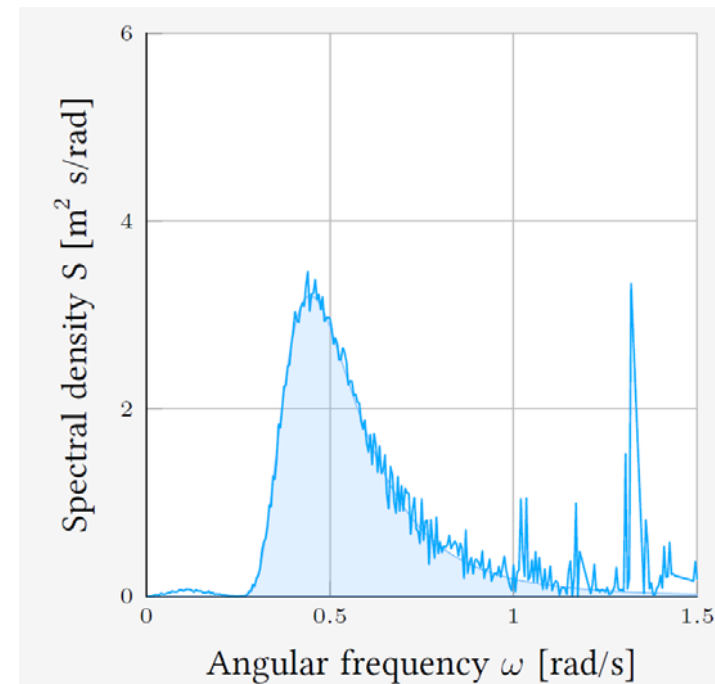
# Time domain procedures

- ÷ Time domain procedures still need further developments, but promising results have been obtained from simulations

## Wave estimation using Kalman filtering:



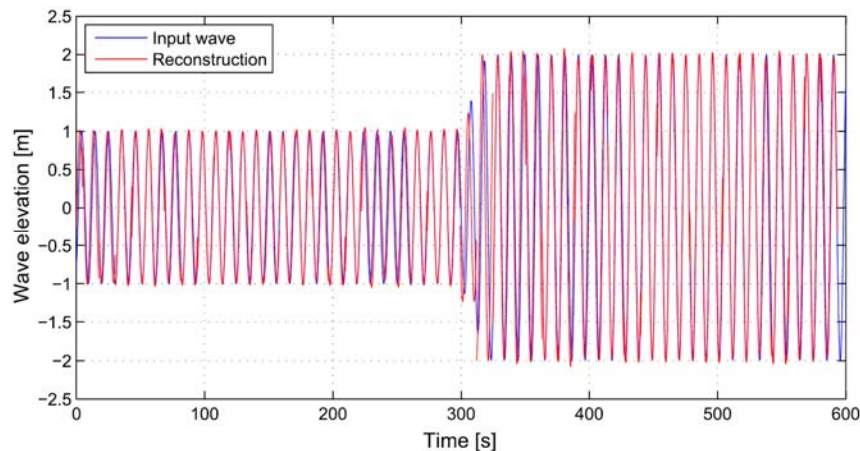
Full lines indicate 'average spectrum', while dashed lines represent lowest and highest energy content in estimated spectrum, obtained from fifty sets of estimations



With forward speed...

# Time domain procedures

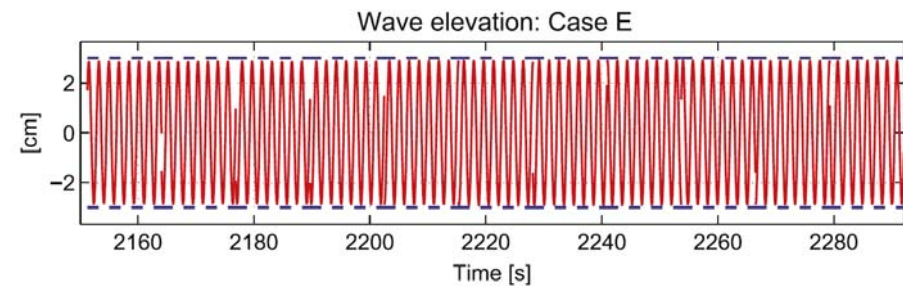
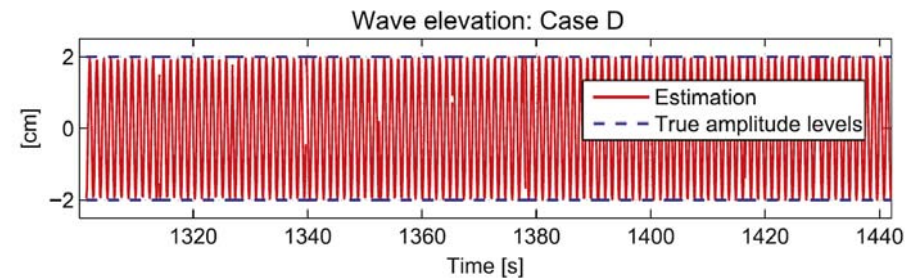
## Nonlinear least squares fitting:



Reconstruction of wave elevation process, running (near) real-time.

### Simulations.

Nielsen et al. (2015)



### Model-scale experiments

Nielsen et al. (2016)



# Conclusions and further work

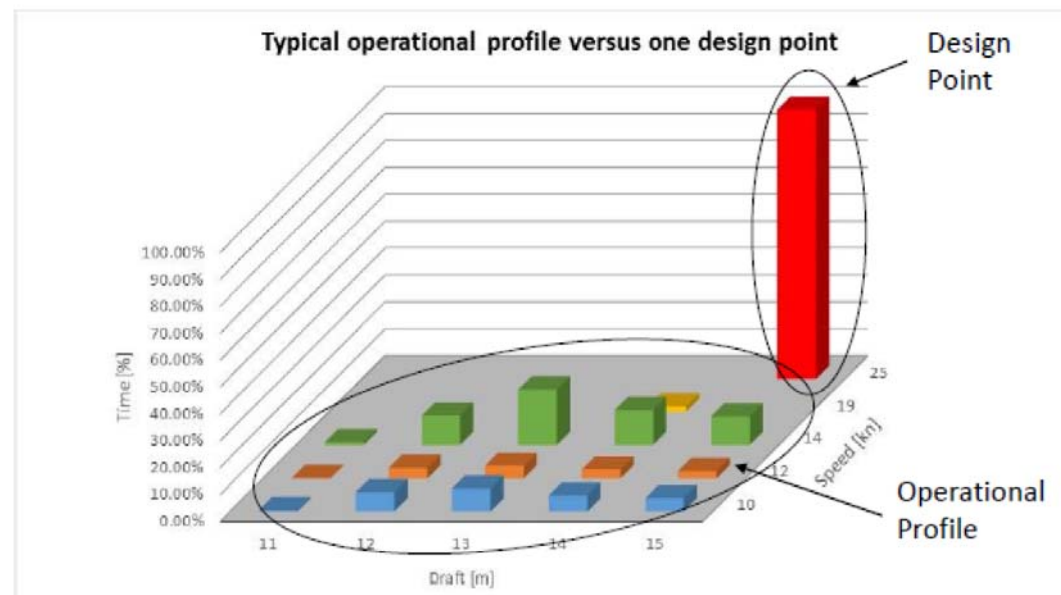
- Well-established procedures – in the frequency domain – for sea state estimation; NB: stationary conditions must apply (in principle).
- It is necessary to (further) develop the wave buoy analogy in the time domain to handle truly nonstationary conditions.
- Wave parameter-estimations based entirely on measurements data (procedures exist already for peak period).
- Automatic selection of the best response combination under given operational conditions; a set of three is typically considered.
- Uncertainties are related to both measurements and transfer functions; i.e. uncertainty modelling should be considered to increase reliability.
- Fault-detection and fault-tolerant approaches
- Global network of 'wave recorders'; an enormous amount of wave data/statistics becomes available if all ships navigating the oceans collect data
- ... ..

# Conclusions and further work

## Other uses of shipboard SSE

- Study ships' operational profiles in a short-term sense and during their lifetime; do ships meet the wave scenarios as they were designed for?
- Added resistance in waves; improved models for added resistance in waves and experimental data is still scarce.
- Investigation of accidents; a sort of 'black box' could be installed on ships, like it is known from the aviation industry, making it easier to investigate weather- and wave-induced accidents.

○ ... ..



# Thank you

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